CS 70 Discrete Mathematics and Probability Theory
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DIS 5A

1 RSA Practice

Bob would like to receive encrypted messages from Alice via RSA.

(a) Bob chooses $p = 7$ and $q = 11$. His public key is (N, e). What is N?

(b) What number is e relatively prime to?

(c) e need not be prime itself, but what is the smallest prime number e can be? Use this value for e in all subsequent computations.

(d) What is $\gcd(e, (p-1)(q-1))$?

(e) What is the decryption exponent d?

(f) Now imagine that Alice wants to send Bob the message 30. She applies her encryption function E to 30. What is her encrypted message?

(g) Bob receives the encrypted message, and applies his decryption function D to it. What is D applied to the received message?

2 Just a Little Proof

Suppose that p and q are distinct odd primes and a is an integer such that $\gcd(a, pq) = 1$. Prove that $a^{(p-1)(q-1)+1} \equiv a \pmod{pq}$.

3 RSA Exponent

What's wrong with using the exponent $e = 2$ in a RSA public key?