

DIS 07B

1 Flippin' Coins

Suppose we have a biased coin, with outcomes H and T , with probability of heads $\mathbb{P}[H] = 3/4$ and probability of tails $\mathbb{P}[T] = 1/4$. Suppose we perform an experiment in which we toss the coin 3 times. An outcome of this experiment is (X_1, X_2, X_3) , where $X_i \in \{H, T\}$.

- (a) What is the *sample space* for our experiment?
- (b) Which of the following are examples of *events*? Select all that apply.
- $\{(H, H, T), (H, H), (T)\}$
 - $\{(T, H, H), (H, T, H), (H, H, T), (H, H, H)\}$
 - $\{(T, T, T)\}$
 - $\{(T, T, T), (H, H, H)\}$
 - $\{(T, H, T), (H, H, T)\}$
- (c) What is the complement of the event $\{(H, H, H), (H, H, T), (H, T, H), (H, T, T), (T, T, T)\}$?
- (d) Let A be the event that our outcome has 0 heads. Let B be the event that our outcome has exactly 2 heads. What is $A \cup B$?
- (e) What is the probability of the outcome (H, H, T) ?
- (f) What is the probability of the event that our outcome has exactly two heads?

2 Venn Diagram

Out of 1000 computer science students, 400 belong to a club (and may work part time), 500 work part time (and may belong to a club), and 50 belong to a club and work part time.

- (a) Suppose we choose a student uniformly at random. Let C be the event that the student belongs to a club and P the event that the student works part time. Draw a picture of the sample space Ω and the events C and P .
- (b) What is the probability that the student belongs to a club?
- (c) What is the probability that the student works part time?
- (d) What is the probability that the student belongs to a club AND works part time?
- (e) What is the probability that the student belongs to a club OR works part time?

3 Shooting Range

You and your friend are at a shooting range. You ran out of bullets. Your friend still has two bullets left but magically lost his gun. Somehow you both agree to put the two bullets into your six-chambered revolver in successive order, spin the revolver, and then take turn shooting. Your first shot was a blank. You want your friend to shoot a blank too, should you spin the revolver again before you hand it to your friend?